mech (se m-IV)

Course Code: PEC401
Time: 2 hour 30 minutes

Course Name : Engineering Mathematics -4 Max. Marks; 80



| $\frac{\text { Q2 }}{}$ | Solve any Four out of Six |
| :---: | :--- |
| A | Obtain Laurent's expansion of $f(z)=\frac{\mathbf{z} \text { marks each }}{z^{2}-2 z-3}$ in (i) $1<\|z\|<3$ (ii) |


|  | $\|z\|>3$ |  |  |
| :---: | :---: | :---: | :---: |
| B | The following results of ranks of were recorded for 11 students. Find Spearman's rank correlation coefficient between the ranks obtained. |  |  |
|  | Pre-module | Post-module |  |
|  | 18 | 22 |  |
|  | 21 | 25 |  |
|  | 16 | 17 |  |
|  | 22 | 24 |  |
|  | 19 | 15 |  |
|  | 24 | 29 |  |
|  | 17 | 20 |  |
|  | 21 | 23 |  |
|  | 23 | 19 |  |
|  | 18 | 20 |  |
|  | 14 | 15 |  |
| C | A person draws 3 balls from a bag containing 7 blue, 5 yellow, 3 purple balls. He is offered Rs, 7, Rs, 5, Rs. 3 if he draws 3 balls of same colour, 2 balls of same colour, 1 ball of each colour respectively. Find his expectation. |  |  |
| D | A brochure inviting subscriptions for a new diet program states that the participants are expected to lose on an average 22 pounds in five weeks. Suppose that, from the data of the five-week weight losses of 26 participants, the sample mean and sample standard deviation are found to be 23.5 and 10.2 , respectively. Could the statement in the brochure be substantiated based on these findings? Test at the $\alpha=0.05$ level of significance. |  |  |
| E | Evaluate using Green's theorem $\int_{c}\left(x^{2} y d x+y^{3} d y\right)$ where $c$ is the boundary of the region bounded by $y=x^{2}$ and $y=x$ from $(0,0)$ to $(1,1)$ then to $(0,0)$ traversed in positive sense |  |  |
| F | Show that the vector, $\bar{F}=\left(x^{2}-y z\right) i+\left(y^{2}-x z\right) j+\left(z^{2}-x y\right) k$ is irrotational and hence, find $\emptyset$ such that $\bar{F}=\nabla \emptyset$. |  |  |
| Q3 | Solve any Four out of Six - 5 marks each |  |  |
| A | The IQs of individuals admitted to a state school for the mentally retarded are approximately normally distributed with a mean of 60 and a standard deviation of 10 . <br> (a) What is the probability that an individual picked at random will have an IQ between 55 and 75 ? (b) what is the lowest IQ of top $30 \%$ individuals? |  |  |
| B | If the mean age at death of 64 men engaged in an occupation is 52.4 years with standard deviation of $10 \cdot 2$ years, what are the $98 \%$ confidence limits for the mean age of all men in that population? <br> Also determine can it be safely assume at $5 \%$ level oŕ significance that that mean age of death of population is 56 ? |  |  |
| C | If the directional derivative of $\emptyset=a x^{2}+b y+2 z$ at $(1,1,1)$ is maximum in the direction of $i+j+k$, find a and b . |  |  |
| D | Evaluate $\int_{c} \frac{(12 z-7) d z}{(z-1)^{2}(2 z+3)}$, where $c$ is the circie (i) $\|z+i\|=\sqrt{3}$ |  |  |



