

Duration : 3 Hrs**Maximum Marks : 80**

Note:

- 1) Question No 1 is compulsory.
- 2) Solve any three questions out of remaining five questions.

Q.1) Solve any 4 20

- 1) Derive the complexity of quick sort for best case and worst case.
- 2) What is asymptotic analysis? Define Big O, Omega and Theta notations.
- 3) Write an algorithm to find all pairs shortest path using dynamic programming.
- 4) Write a note on "Optimal Storage on Tapes".
- 5) Define master theorem. Solve the following using master method.
 $T(n) = 8T(n/2) + n^2$

Q.2. A) Write an algorithm for finding minimum and maximum using divide and conquer. Also derive its complexity. 10**B) Write Kruskal's algorithm and show its working by taking suitable example of graph with 5 vertices. 10****Q.3. A) Solve fractional knapsack problem for the following. 10**
 $n=6, p=(18, 5, 9, 10, 12, 7) \quad w=(7, 2, 3, 5, 3, 2)$
B) Write an algorithm for Knuth Morris Pratt (KMP) pattern matching. 10**Q.4. A) Write an algorithm to solve N Queens problem. Show its working for N = 4. 10****B) Write an algorithm to solve sum of subset problem and solve the following problem. $n=4, w = \{4, 5, 8, 9\}$, required sum = 9. 10****Q.5. A) Prove that Vertex Cover problem is NP Complete. 10****B) Find the longest common subsequence for the following two strings. 10**

X=ABACABB Y= BAB CAB

Q.6) Write short note on any 2. 20

- (a) Assembly Line Scheduling
- (b) Job Sequencing with Deadlines
- (c) 15 Puzzle Problem (d) P, NP and NPC Classes
