

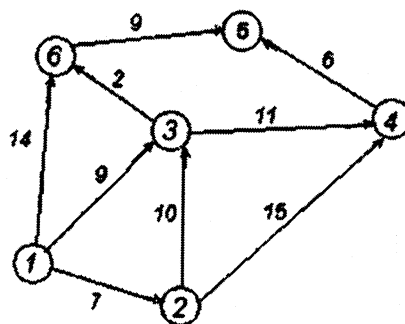
(3 Hours)

[Total Marks: 80]

N.B.: (1) Question No.1 is compulsory.

(2) Attempt **any three** questions from the remaining **five** questions.(3) Make **suitable** assumptions wherever **necessary** but **justify your assumptions**.

- 1 a) Define the asymptotic notations used for best case, average case, and worst case analysis of algorithm. [05]
- b) Solve the following recurrence relations using master's method [05]
 - i. $T(n) = T(n/2) + 2^n$
 - ii. $T(n) = 4T(n/2) + n/\log n$
- c) Explain the properties of red-black trees. [05]
- d) Explain the Line Segment properties. [05]
- 2 a) Explain insertion and deletion algorithms in Red-Black trees with examples. [10]
- b) Find an optimal parenthesization of a matrix chain product whose sequence of dimension is {4, 1, 1, 4, 1, 1, 3}. [10]
- 3 a) What is Binomial Heap? Explain the operations that can be carried out on Binomial Heap with example. [10]
- b) Explain maximum bipartite matching algorithm with an example. [10]
- 4 a) Explain the relabel to front algorithm for finding maximum flow with an example. [10]
- b) Find the shortest path from node 1 to all other nodes using Dijkstra's algorithm. [10]



- 5 a) Use Simplex method to solve the following objective function [10]

Max $Z = 3x_1 - x_2$,
 Subject to
 $2x_1 + x_2 \geq 2$
 $x_1 + 3x_2 \leq 3$
 $x_2 \leq 4$
 where $x_1, x_2, x_3 \geq 0$
- b) Explain insertion and deletion in B-tree with an example. [10]
- 6 a) Discuss the Jarvis March algorithm for finding the convex hull. [10]
- b) Explain the Closest Pair of Points using divide and conquer. [10]